

Program Analysis

Call Graphs

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Slides adapted from Eric Bodden

Warm-up Quiz

What does this Java code print?

```
class Reflection {
    static class Car {
        private String color;
        protected void getColor() {
            System.out.println("A "+color+" car");
        }
    }
}
public static void main(String[] args)
    throws Exception {
    Class clazz = Class.forName("Reflection$Car");
    Car car = (Car) clazz.newInstance();
    Method getColor = clazz.getDeclaredMethod("getColor");
    getColor.invoke(car);
}
}
```

Warm-up Quiz

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        private String color;
        protected void getColor() {
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        Class clazz = Class.forName("Reflection$Car");
        Car car = (Car) clazz.newInstance();
        Method getColor = clazz.getDeclaredMethod("getColor");
        getColor.invoke(car);
    }
}
```

Result: A null car

Call Graph Analysis

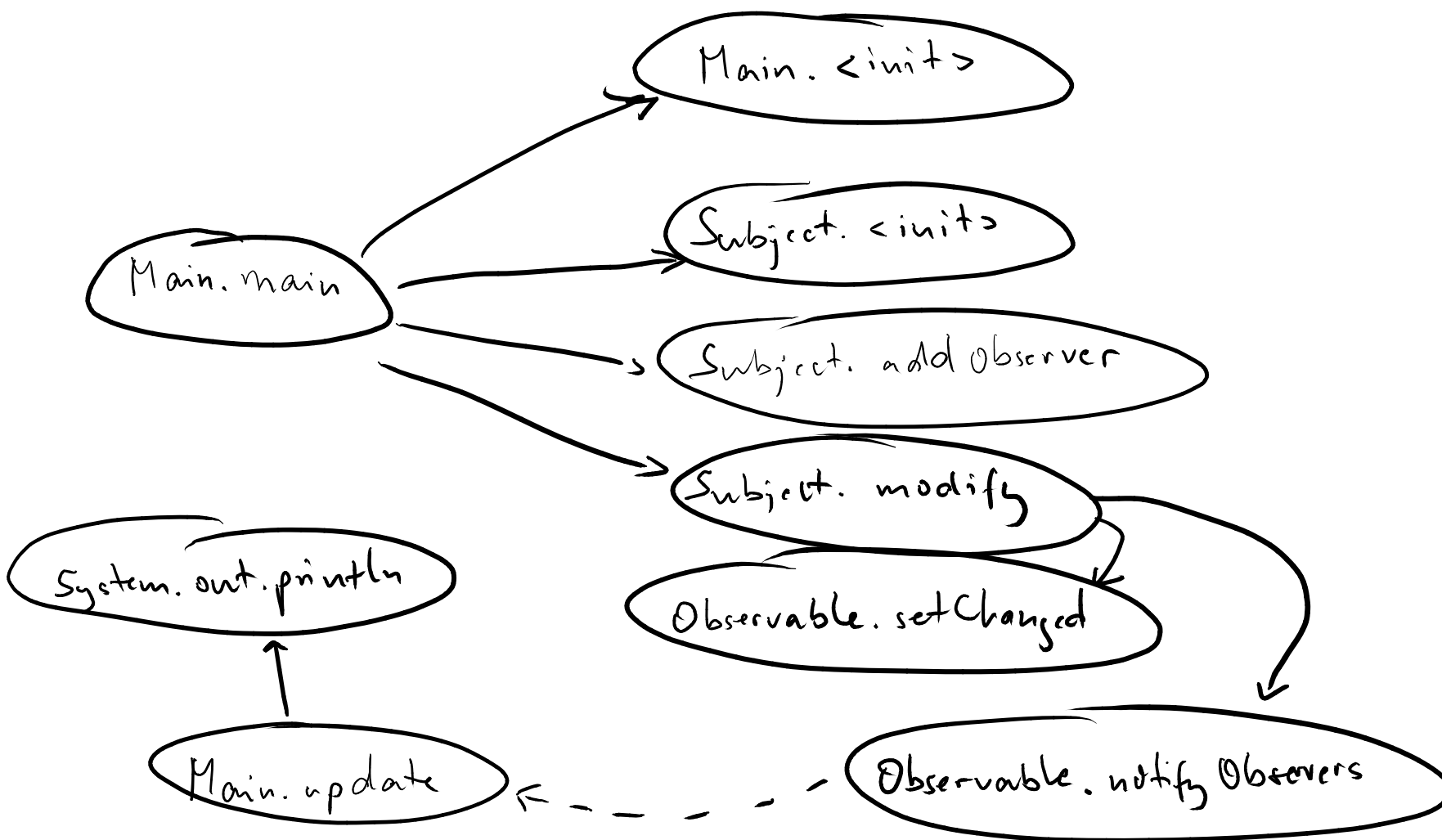
- **Call graph**: Abstraction of all method calls in a program
 - Nodes: **Methods**
 - Edges: **Calls**
 - **Flow-insensitive**: No execution order
- **Here: Static call graph**
 - Abstract of all calls that **may** execute

Example

```
public class Main implements Observer {
    public static void main(String[] args) {
        Main m = new Main();
        Subject s = new Subject();
        s.addObserver(m);
        s.modify();
    }

    public void update(Observable o, Object arg) {
        System.out.println(o+" notified me!");
    }

    static class Subject extends Observable
        public void modify() {
            setChanged();
            notifyObservers();
        }
}
```

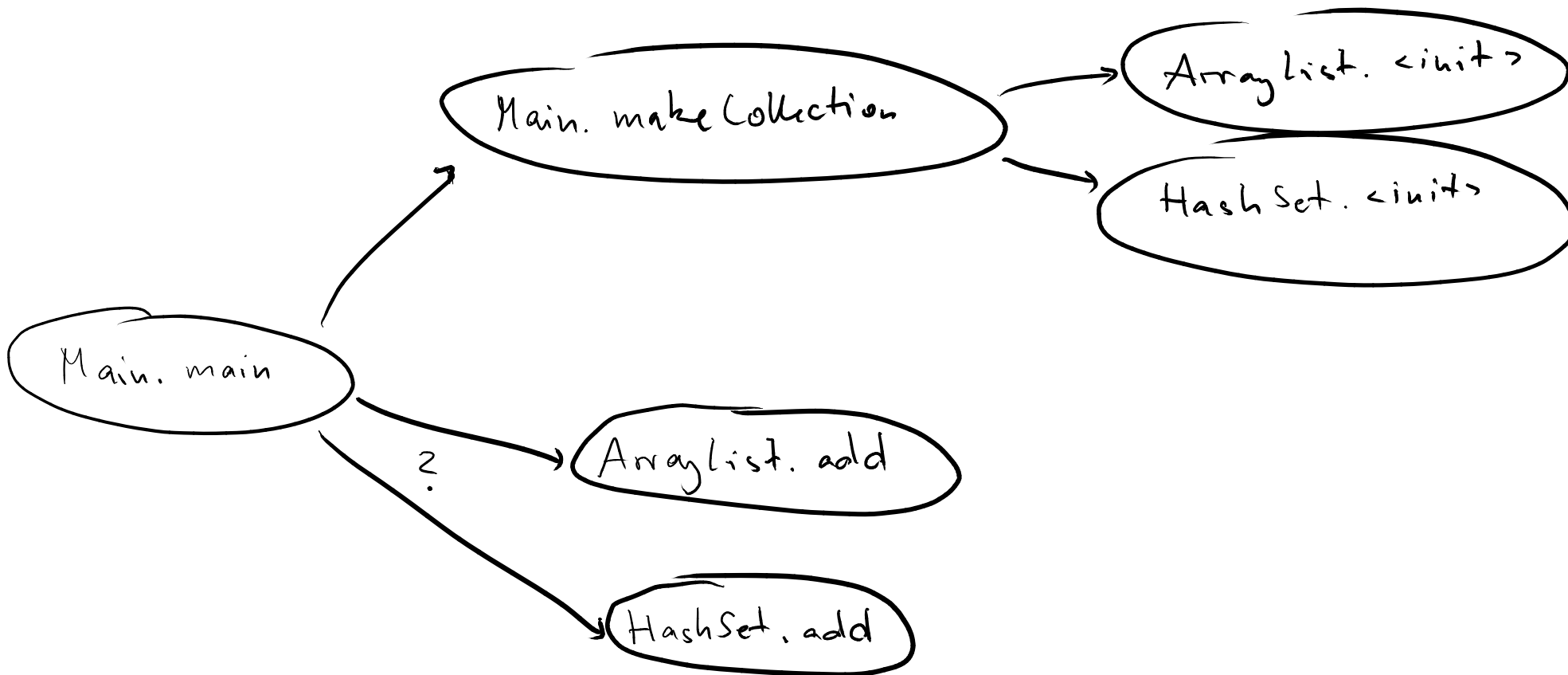


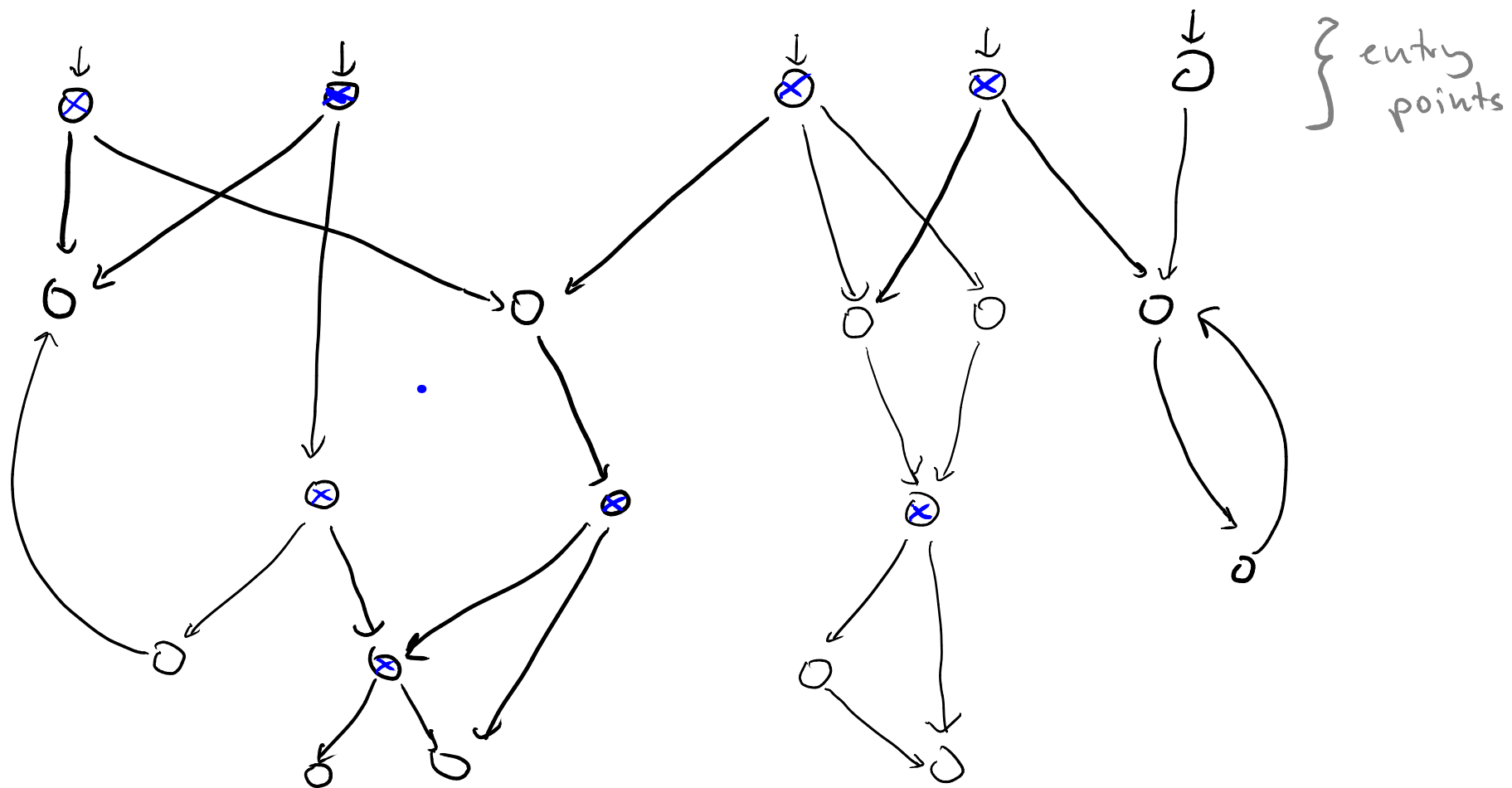
Problem: Polymorphic Calls

```
import java.util.*;

public class Main {
    public static void main(String[] args) {
        Collection c = makeCollection(args[0]);
        c.add("hello");
    }

    static Collection makeCollection(String s) {
        if(s.equals("list")) {
            return new ArrayList();
        } else {
            return new HashSet();
        }
    }
}
```

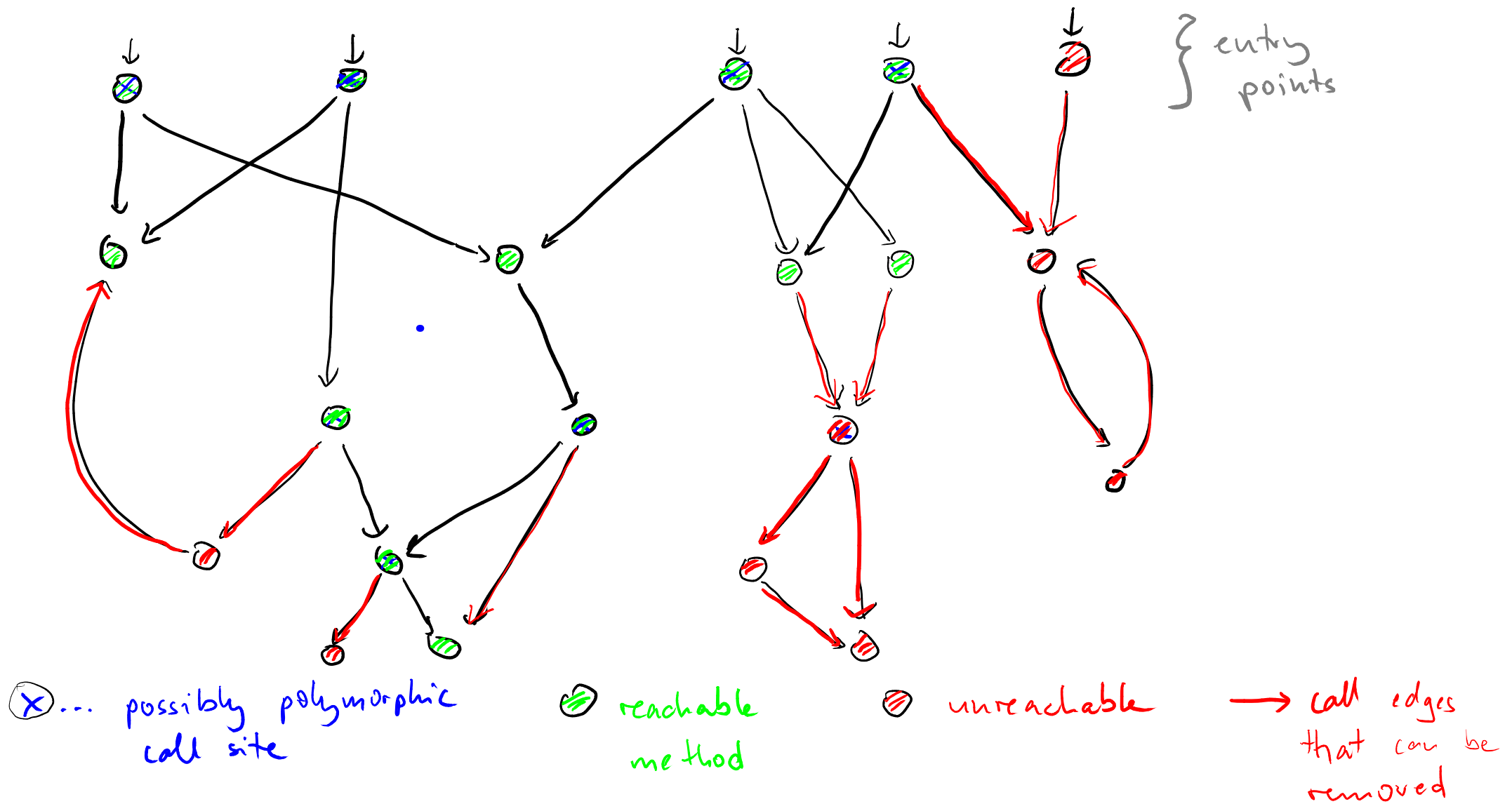




X ... possibly polymorphic
call site

Improving the Call Graph

- **Prune graph:**
Focus on feasible behavior
- **Want to minimize**
 - Reachable methods
 - Call edges
 - Potentially polymorphic call sites



Overview

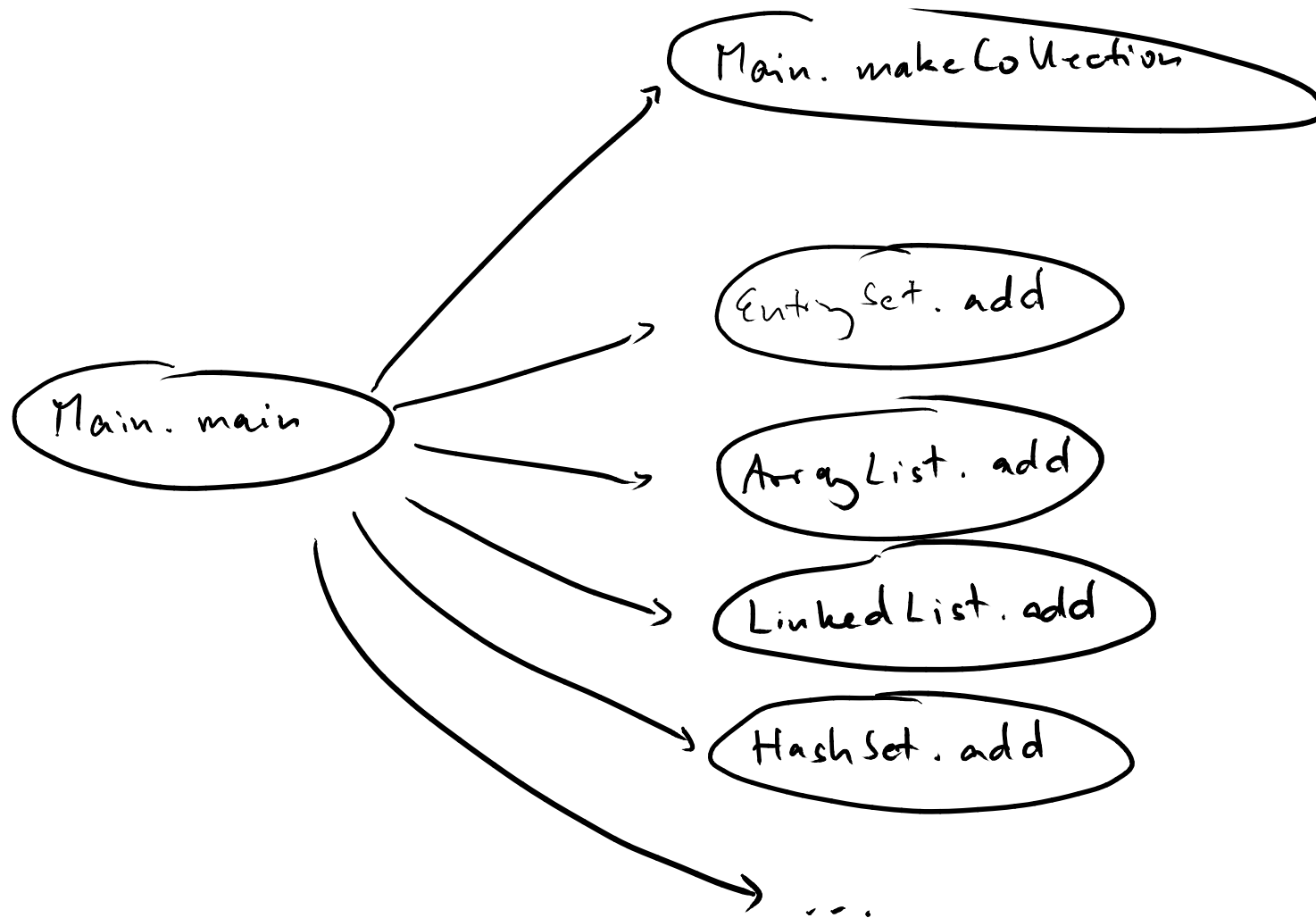
- Introduction
- Simple & efficient: CHA, RTA ←
- Analyzing assignments: VTA, DTA
- Call graphs and points-to analysis:
Spark

Five Algorithms

- **Many algorithms for call graph construction**
 - Class hierarchy analysis (CHA)
 - Rapid type analysis (RTA)
 - Variable type analysis (VTA)
 - Declared type analysis (DTA)
 - General construction framework: Spark

Class Hierarchy Analysis (CHA)

- Most simple analysis
- For a polymorphic call site $m()$ on declared type T :
Call edge to $T.m$ and **any subclass of T that implements m**



Class Hierarchy Analysis (CHA)

■ Pros

- Very **simple**
- **Correct**: Contains edges for all calls that the program may execute
- **Few requirements**: Needs only hierarchy, no other analysis information

■ Cons

- **Very imprecise**: Most edges will never be executed

Rapid Type Analysis (RTA)

- Like CHA, but:
Take into account only those **types**
that the program actually instantiates

Problem: Polymorphic Calls

```
import java.util.*;

public class Main {
    public static void main(String[] args) {
        Collection c = makeCollection(args[0]);
        c.add("hello");
    }

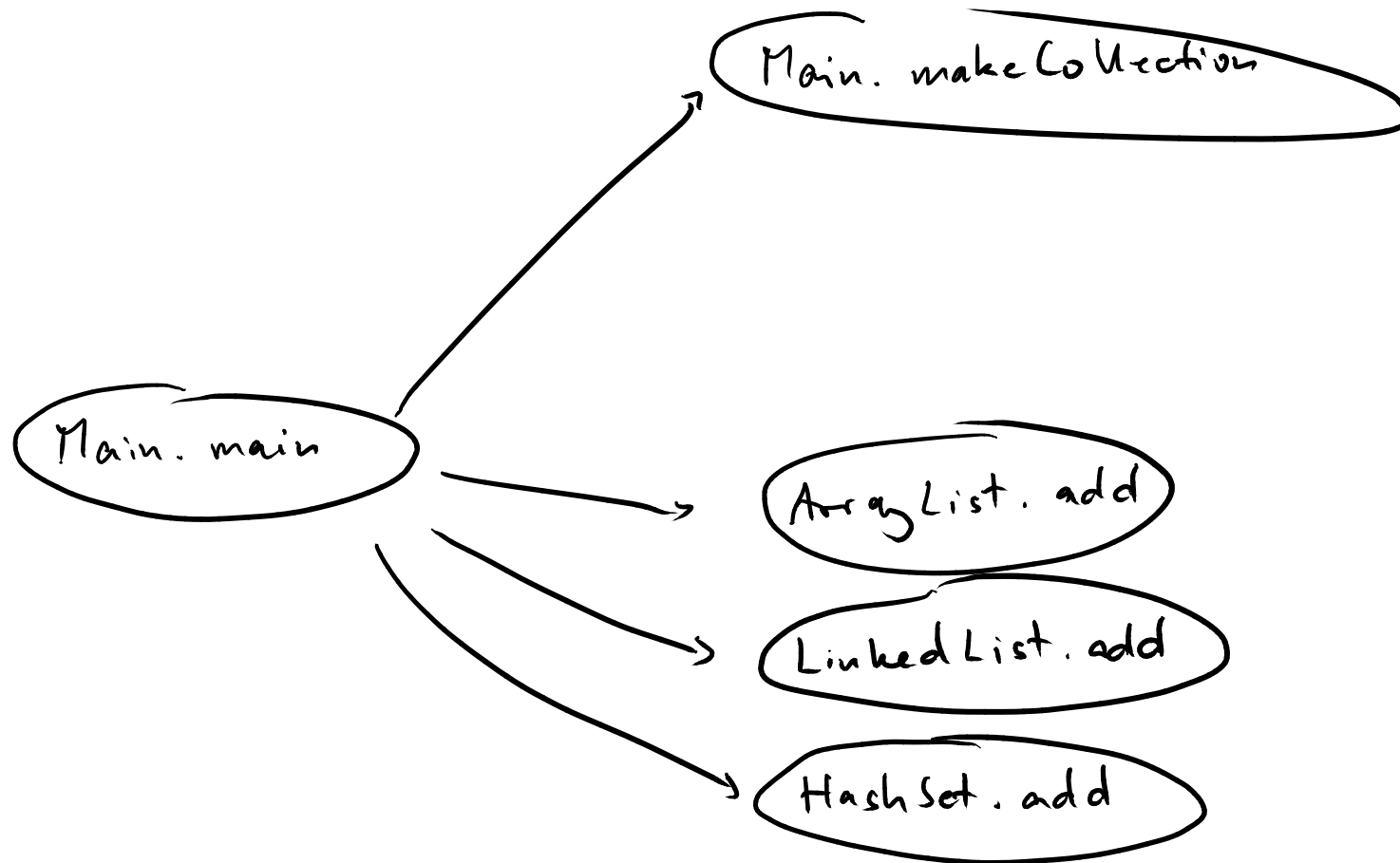
    static Collection makeCollection(String s) {
        if(s.equals("list")) {
            return new ArrayList();
        } else {
            return new HashSet();
        }
    }
}
```

Problem: Polymorphic Calls

```
import java.util.*;

public class Main {
    public static void main(String[] args) {
        Collection c = makeCollection(args[0]);
        c.add("hello");
        new LinkedList();
    }

    static Collection makeCollection(String s) {
        if(s.equals("list")) {
            return new ArrayList();
        } else {
            return new HashSet();
        }
    }
}
```



Rapid Type Analysis (RTA)

■ Pros

- **Still pretty fast**: Complexity is $\mathcal{O}(|Program|)$

- **Correct**

- **Much more precise** than CHA:

 - Many unnecessary nodes and edges pruned

■ Cons

- Doesn't reason about **assignments**

Overview

- **Introduction**
- **Simple & efficient: CHA, RTA**
- **Analyzing assignments: VTA, DTA** ←
- **Call graphs and points-to analysis:
Spark**

Variable Type Analysis (VTA)

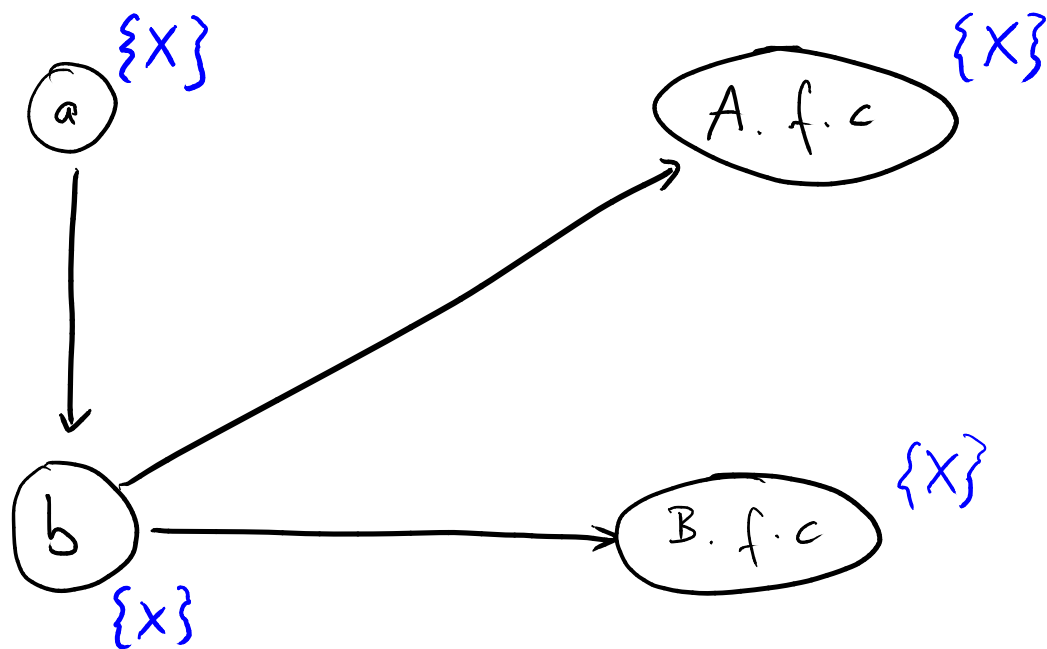
- Reason about **assignments**
- Infer what **types the objects involved in a call may have**
- Prune calls that are infeasible based on the inferred types

Example

```
a = new X();  
...  
b = a;  
...  
o.f(b);
```

```
public class A {  
    public void f(C c) {  
        c.m();  
    }  
}
```

```
public class B {  
    public void f(C c) {  
        c.m();  
    }  
}
```

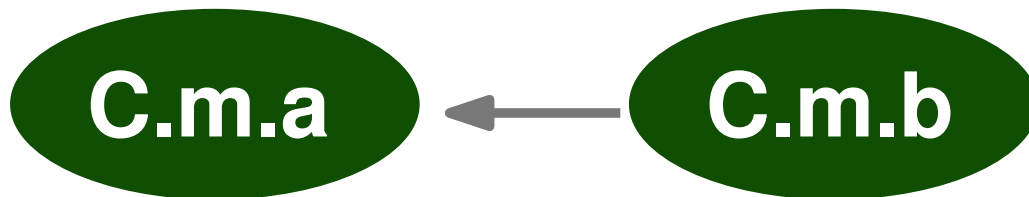
Type Propagation

Four steps:

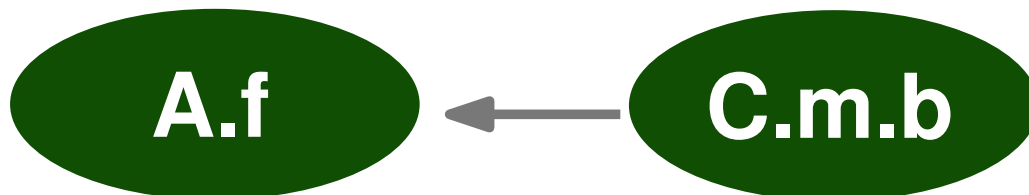
- Form **initial conservative call graph**
 - E.g., using CHA or RTA
- Build **type-propagation graph**
- **Collapse** strongly connected components
- **Propagate types** in one iteration

Building Type Propagation Graph

- Assume statement $a = b;$ is in method $C.m$



- Assume another statement $a.f = b;$ where field f is declared in A



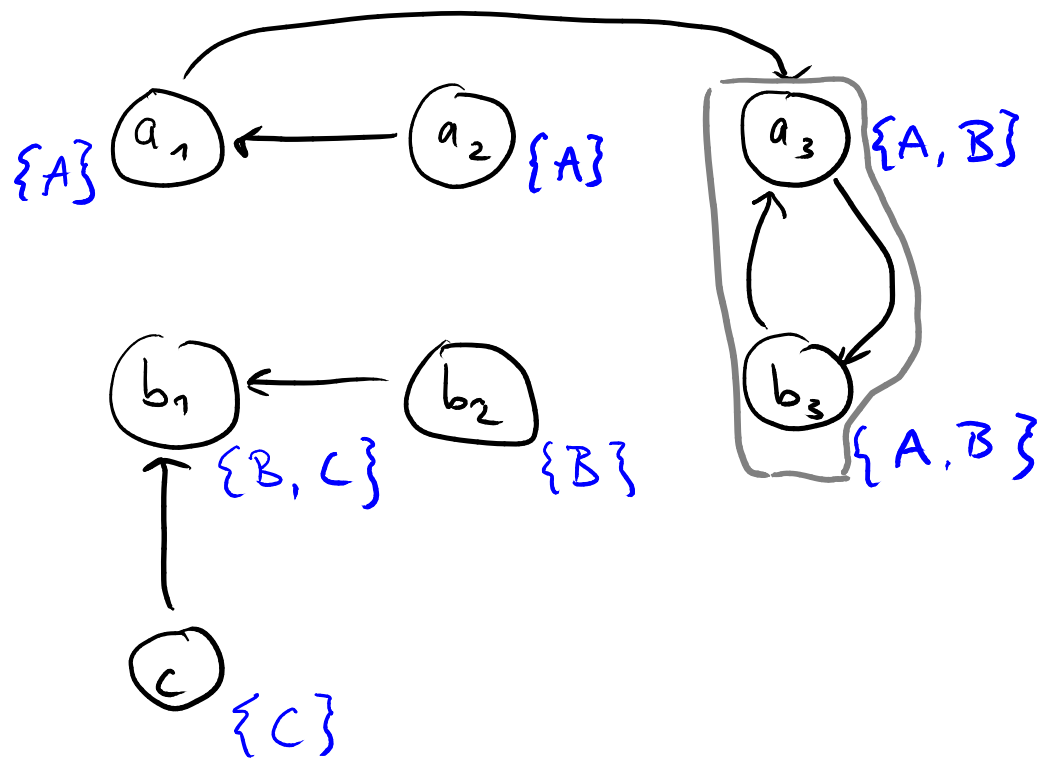
Example

```
A a1, a2, a3; B b1, b2, b3; C c;
```

```
a1 = new A();  
a2 = new A();  
a3 = new B();  
b1 = new B();  
b2 = new B();  
b3 = new B();  
c = new C();
```

```
a1 = a2;  
b3 = (B) a3;  
a3 = b3;  
a3 = a1;  
b1 = b2;  
b1 = c;
```

A
↑
B
↓
C



Side Note: Field Representations

How does the analysis represent $a.f$?

- **Field-sensitive**: Represented as $a.f$
- **Field-insensitive**: Represented as $a.*$ or a
- **Field-based**: Represented as $A.f$, where A is class of a

Side Note: Field Representations

How does the analysis represent $a . f$?

- **Field-sensitive**: Represented as $a . f$
- **Field-insensitive**: Represented as $a . *$ or a
- **Field-based**: Represented as $A . f$, where A is class of a

VTA is field-based

Variable Type Analysis (VTA)

■ Pros

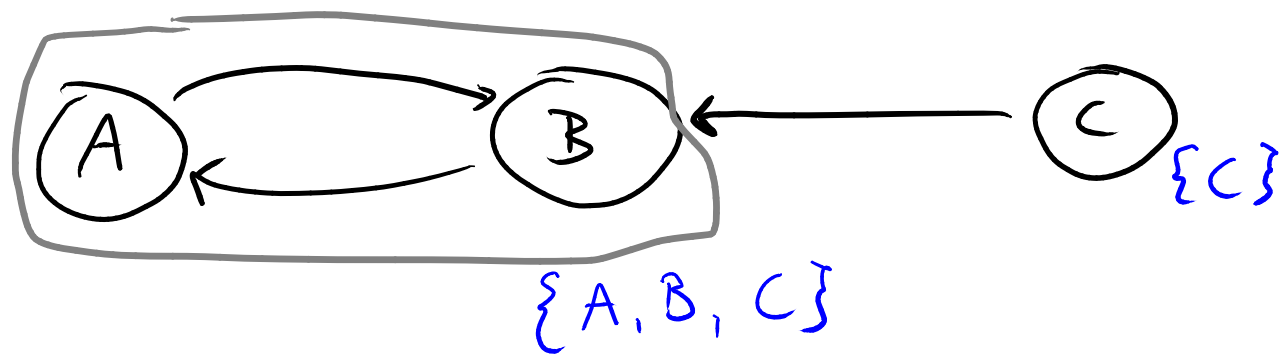
- **More precise than RTA**: Considers only those types that may actually reach the call site
- Still **relatively fast**

■ Cons

- **Requires initial call graph** (i.e., actually a refinement algorithm)
- **Some imprecision** remains, e.g., because of field-based analysis

Declared-Type Analysis (DTA)

- **“Small brother of VTA”**
- **Also reasons about assignments and how they propagate types**
- **But: Not per variable, but **per type****



Declared-Type Analysis (DTA)

■ Pros

- **Faster than VTA**: Graph is smaller, propagation is faster
- **More precise than RTA**

■ Cons

- **Less precise than VTA**: Does not distinguish variables of same type

Overview

- Introduction
- Simple & efficient: CHA, RTA
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Spark: Idea

- **RTA, DTA, and VTA: Instances of one **single unifying framework****
- **General recipe**
 - First, built **pointer-assignment graph** (PAG)
 - **Propagate information** through graph
- **Combine call graph construction with **points-to analysis****
 - Reason about objects a variable may refer to

Pointer-Assignment Graph (PAG)

■ Nodes

- Allocation
- Variable
- Field reference

■ Edges

- Allocation
- Assignment
- Field store
- Field load

Pointer-Assignment Graph (PAG)

■ Nodes

- Allocation →
- Variable
- Field reference

- One for each **new A()**
- Represents a **set of objects**
- Has an **associated type**, e.g., **A**


■ Edges

- Allocation
- Assignment
- Field store
- Field load

alloc₁

Pointer-Assignment Graph (PAG)

■ Nodes

- Allocation
- Variable 
- Field reference

■ Edges

- Allocation
- Assignment
- Field store
- Field load

- One for each **local variable, parameter, static field, and thrown exception**

- Represents a memory location holding **pointers to objects**

- May be typed (depends on setting)



Pointer-Assignment Graph (PAG)

■ Nodes

- Allocation
- Variable
- Field reference →

■ Edges

- Allocation
- Assignment
- Field store
- Field load

■ One for each $p.f$

■ Represents a **pointer dereference**

■ Has a variable node as its base, e.g., p

■ Also models contents of arrays:

$a.<elements>$


$p.f$

Pointer-Assignment Graph (PAG)

■ Nodes

- Allocation
- Variable
- Field reference

■ Edges

- Allocation 
- Assignment
- Field store
- Field load

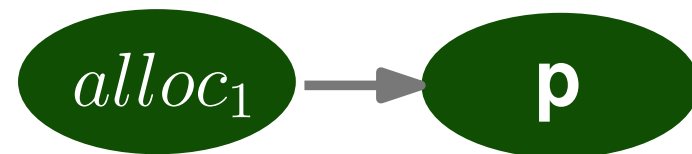
- Represents **allocation** of an object **assigned** to a **variable**

- E.g., for

```
p = new HashMap();
```

or

```
s = "foo";
```

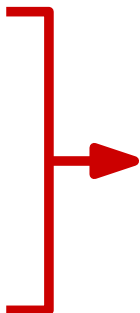


Pointer-Assignment Graph (PAG)

■ Nodes

- Allocation
- Variable
- Field reference

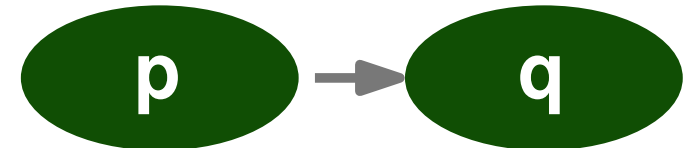
■ Edges

- Allocation
 - Assignment
 - Field store
 - Field load
- 

- Represent **assignments among variables and fields**

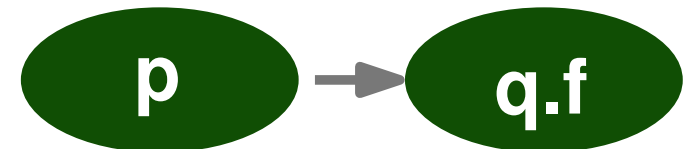
- E.g., for

$q = p;$



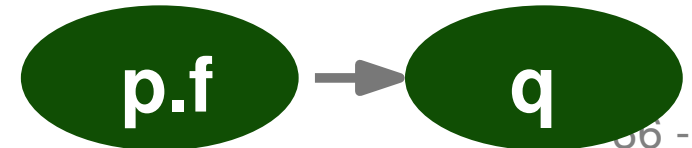
or

$q.f = p;$



or

$q = p.f;$



Example

```
static void foo() {  
    p = new A(); // alloc1  
    q = p;  
    r = new B(); // alloc2  
    p.f = r;  
    t = bar(q);  
    t.m();  
}
```

```
static C bar(C s) {  
    return s.f;  
}
```

Points-to Sets

- For each variable, **set of objects the variable may refer to**

- Objects represented as allocation nodes

- **Example:**

```
a = new X(); // alloc1
```

```
...
```

```
a = new Y(); // alloc2
```

$$pts(a) = \{alloc_1, alloc_2\}$$

Subset-based Analysis

- **Allocation and assignment edges induce subset constraints**

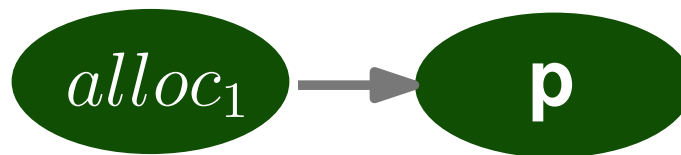
- Reason: Just because we know that

```
p = new A(); // alloc1
```

does not mean that later we cannot see

```
p = new B(); // alloc 2
```

- **Example:**



induces constraint

$$\{alloc_1\} \subseteq pts(p)$$

Subset-based Analysis

- **Allocation and assignment edges induce subset constraints**

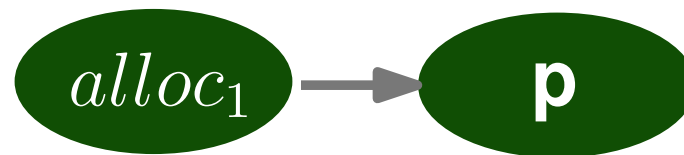
- Reason: Just because we know that

```
p = new A(); // alloc1
```

does not mean that later we cannot see

```
p = new B(); // alloc 2
```

- **Example:**



induces constraint

$$\{alloc_1\} \subseteq pts(p)$$

Note: Analysis is flow-insensitive, i.e., values are never assumed to be overwritten

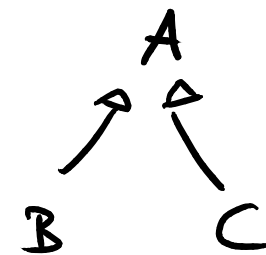
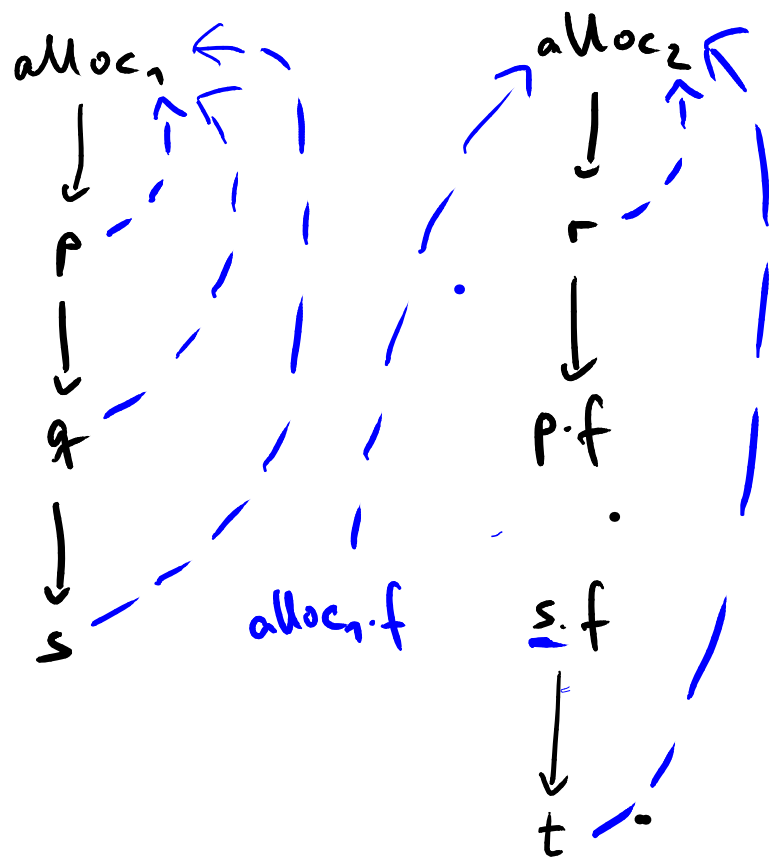
Computing Points-to Sets

- New helper node: **Concrete fields**
- Represents all **objects pointed to by field ϵ** of all objects created at **allocation site**
 - E.g., *alloc₁.f*

Computing Points-to Sets (2)

Iterative propagation algorithm

- **Initialize** $pts(v)$ according to **allocation edges**
- Repeat until no changes
 - **Propagate** sets along **assignment edges** $a \rightarrow b$
 - For each **load edge** $a.f \rightarrow b$:
 - For each $c \in pts(a)$, **propagate** $pts(c.f)$ to $pts(b)$
 - For each **store edge** $a \rightarrow b.f$:
 - For each $c \in pts(b)$, **propagate** $pts(a)$ to $pts(c.f)$



(all $t.m()$ goes to $B.m()$)

---> points to

Simpler Variants

- **Spark framework supports many variants**
 - Just one allocation site per type
 - Fields simply represented by their signature
 - Equality instead of subsets for assignments
 - Etc.

Spark

■ Pros

- **Generic algorithm** where precision and efficiency can be tuned
- Jointly computing **call graph and points-to sets** increases precision

■ Cons

- Still **flow-insensitive**
- Can be quite **expensive** to compute

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- **Analyzing assignments: VTA, DTA**
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Spark**

