

# **Program Analysis – Lecture 8**

## **Symbolic and Concolic Execution**

### **(Part 2)**

**Prof. Dr. Michael Pradel**

**Software Lab, University of Stuttgart**

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# Warm-up Quiz

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What does the following code print?

```
var x = 23;
function f() { console.log(this.x); }
var obj = Object.create({ f: f });
obj.x = 42;
f();
obj.f();
```

23

42

23

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23

42

42

23

# Warm-up Quiz

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What does the following code print?

```
var x = 23;
function f() { console.log(this.x); }
var obj = Object.create({ f: f });
obj.x = 42;
f();
obj.f();
```

**obj's prototype  
has method f**



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23

# Warm-up Quiz

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What does the following code print?

```
var x = 23;
function f() { console.log(this.x); }
var obj = Object.create({ f: f });
obj.x = 42;
f();
obj.f();
```

**this is determined at call site:**

- Simple call: global
- Object method: base object

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23

# Outline

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1. Classical **Symbolic Execution**
2. **Challenges** of Symbolic Execution
3. **Concolic Testing** ←
4. Large-Scale Application in **Practice**

Mostly based on these papers:

- *DART: directed automated random testing*, Godefroid et al., PLDI'05
- *KLEE: Unassisted and Automatic Generation of High-Coverage Tests for Complex Systems Programs*, Cadar et al., OSDI'08
- *Automated Whitebox Fuzz Testing*, Godefroid et al., NDSS'08

# Concolic Testing

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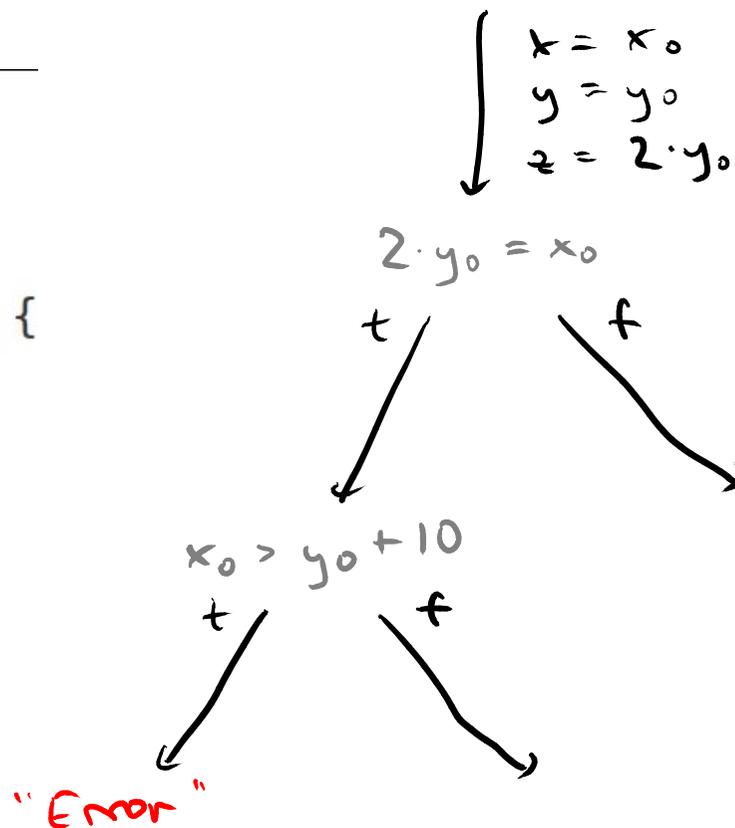
**Mix concrete and symbolic execution =  
"concolic"**

- Perform concrete and symbolic execution side-by-side
- Gather path constraints while program executes
- After one execution, negate one decision, and re-execute with new input that triggers another path

## Symbolic execution

```
function double(n) {
  return 2 * n;
}
```

```
function testMe(x, y) {
  var z = double(y);
  if (z === x) {
    if (x > y + 10) {
      throw "Error";
    }
  }
}
```



Execution 1:Concrete  
executionSymbolic  
executionPath  
conditions

```
function double(n) {
  return 2 * n;
}
```

```
function testMe(x, y) {
  var z = double(y);
  if (z === x) {
    if (x > y + 10) {
      throw "Error";
    }
  }
}
```

 $x = 22, y = 7$ 
 $x = x_0, y = y_0$ 
 $x = 22, y = 7,$   
 $z = 14$ 
 $x = x_0, y = y_0$   
 $z = 2 \cdot y_0$ 
 $x = 22, y = 7,$   
 $z = 14$ 
 $x = x_0, y = y_0,$   
 $z = 2 \cdot y_0$ 
 $2 \cdot y_0 \neq x_0$ 
Solve:  $2 \cdot y_0 = x_0$ Solution:  $x_0 = 2, y_0 = 1$

Execution 2:Concrete  
executionSymbolic  
executionPath  
conditions

```
function double(n) {
  return 2 * n;
}
```

```
function testMe(x, y) {
  var z = double(y);
  if (z === x) {
    if (x > y + 10) {
      throw "Error";
    }
  }
}
```

 $x = 2, y = 1$  $x = x_0, y = y_0$  $x = 2, y = 1,$   
 $z = 2$  $x = x_0, y = y_0,$   
 $z = 2 \cdot y_0$ 

"

"

 $2 \cdot y_0 = x_0$ 

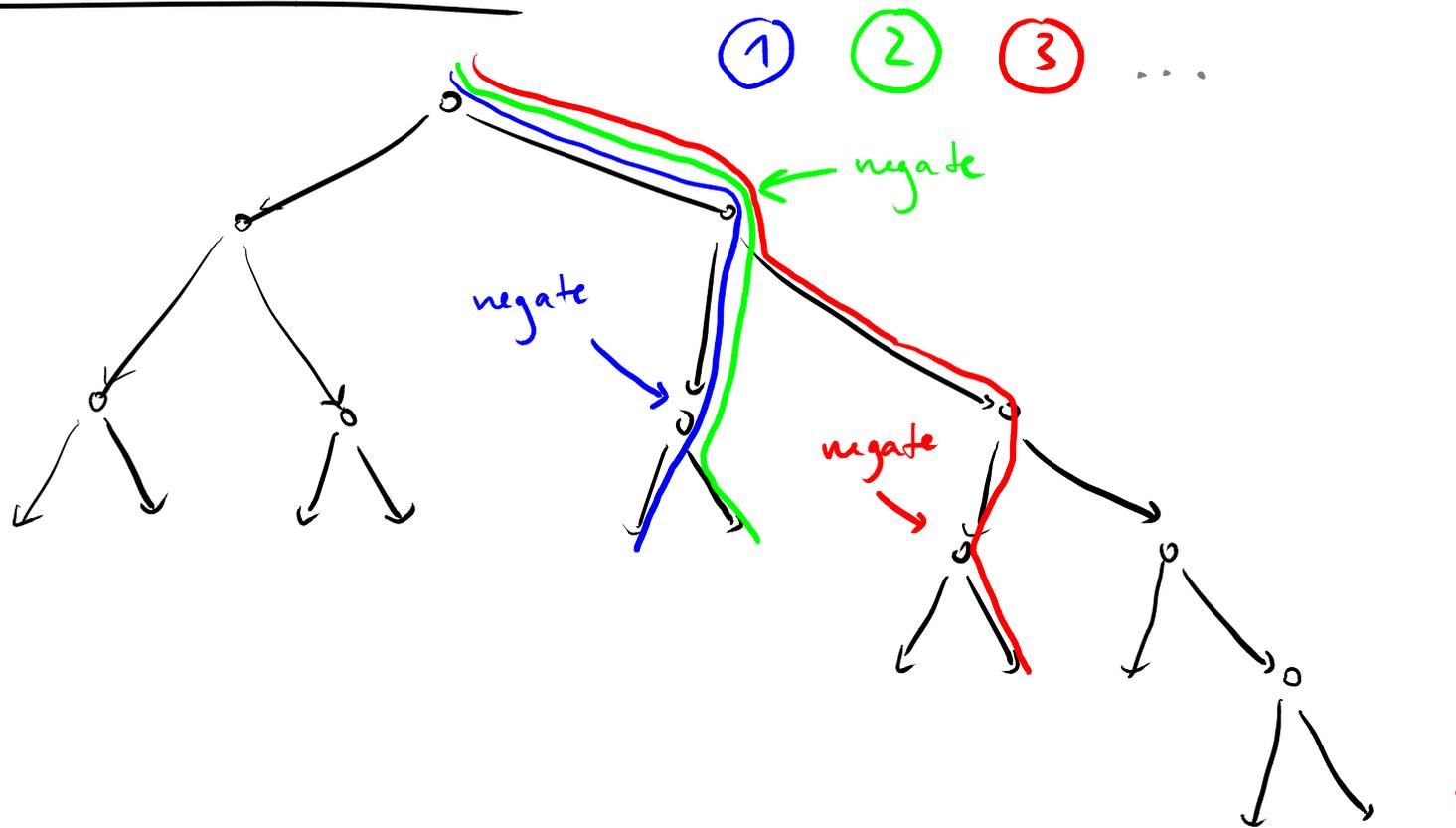
"

"

 $2 \cdot y_0 = x_0 \wedge$   
 $x_0 \leq y_0 + 10$ Solve:  $2 \cdot y_0 = x_0 \wedge x_0 > y_0 + 10$ Solution:  $x_0 = 30, y_0 = 15$ 

Hits "Error"

## Exploring the execution tree



# Algorithm

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## Repeat until all paths are covered

- **Execute** program with concrete input  $i$  and collect **symbolic constraints** at branch points:  $C$
- **Negate one constraint** to force taking an alternative branch  $b'$ : Constraints  $C'$
- Call constraint solver to **find solution** for  $C'$ : **New concrete input**  $i'$
- **Execute** with  $i'$  to take branch  $b'$
- Check at runtime that  $b'$  is indeed taken  
Otherwise: "divergent execution"

## Divergent execution: Example

```
function f(a) {
  if (Math.random() < 0.5) {
    if (a > 1) {
      console.log("took it");
    }
  }
}
```

First execution

$a = 0$

branch taken

branch not taken

path constraint:

$a_0 \leq 1$

negate & solve:

$a_0 = 2$

Second execution

$a = 2$

branch not taken

→ Divergent execution

# Quiz

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After how many executions and how many queries to the solver does concolic testing find the error?

Initial input:  $a=0$ ,  $b=0$

```
function concolicQuiz(a, b) {  
  if (a === 5) {  
    var x = b - 1;  
    if (x > 0) {  
      console.log("Error");  
    }  
  }  
}
```

# Benefits of Concolic Approach

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When symbolic reasoning is impossible or impractical, **fall back to concrete values**

- Native/system/API functions
- Operations not handled by solver (e.g., floating point operations)

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# Large-Scale Concolic Testing

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- **SAGE**: Concolic testing tool developed at Microsoft Research
- Test robustness against unexpected **inputs read from files**, e.g.,
  - Audio files read by media player
  - Office documents read by MS Office
- Start with known input files and handle **bytes read from files as symbolic input**
- Use concolic execution to compute variants of these files

# Large-Scale Concolic Testing (2)

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- Applied to hundreds of applications
- Over **400 machine years of computation** from 2007 to 2012
- Found **hundreds of bugs**, including many security vulnerabilities
  - One third of all the bugs discovered by file fuzzing during the development of Microsoft's Windows 7

# Summary: Symbolic & Concolic Testing

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## Solver-supported, whitebox testing

- Reason **symbolically** about (parts of) inputs
- Create new inputs that **cover not yet explored paths**
- More **systematic** but also more **expensive** than random and fuzz testing
- **Open challenges**
  - Effective exploration of huge search space
  - Other applications of constraint-based program analysis, e.g., debugging and automated program repair