

# **Program Testing and Analysis: Slicing (Part 2)**

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# Warm-up Quiz

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What does the following code print?

```
var x = 23;
function f() { console.log(this.x); }
var obj = Object.create({ f: f });
obj.x = 42;
f();
obj.f();
```

23

42

23

42

23

42

42

23

# Warm-up Quiz

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What does the following code print?

```
var x = 23;
function f() { console.log(this.x); }
var obj = Object.create({ f: f });
obj.x = 42;
f();
obj.f();
```

**obj's prototype  
has method f**



23

42

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42

23

# Warm-up Quiz

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What does the following code print?

```
var x = 23;
function f() { console.log(this.x); }
var obj = Object.create({ f: f });
obj.x = 42;
f();
obj.f();
```

**this is determined at call site:**

- Simple call: global
- Object method: base object

23

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23

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42

23

# Slicing: Outline

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1. Introduction

2. Static Slicing

3. Thin Slicing

4. Dynamic Slicing ←

Mostly based on these papers:

- *Program Slicing*, Weiser., IEEE TSE, 1984
- *Thin Slicing*, Sridharan et al., PLDI 2007
- *Dynamic Program Slicing*, Agrawal and Horgan, PLDI 1990
- *A Survey of Program Slicing Techniques*, Tip, J Prog Lang 1995

# Dynamic Slice (Simple Approach)

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- **Given: Execution history**
  - Sequence of PDG nodes that are executed
- **Slice for statement  $n$  and variable  $v$ :**
  - Keep PDG nodes only if there are in history
  - Use static slicing approach (= graph reachability) on reduced PDG

## Example 2

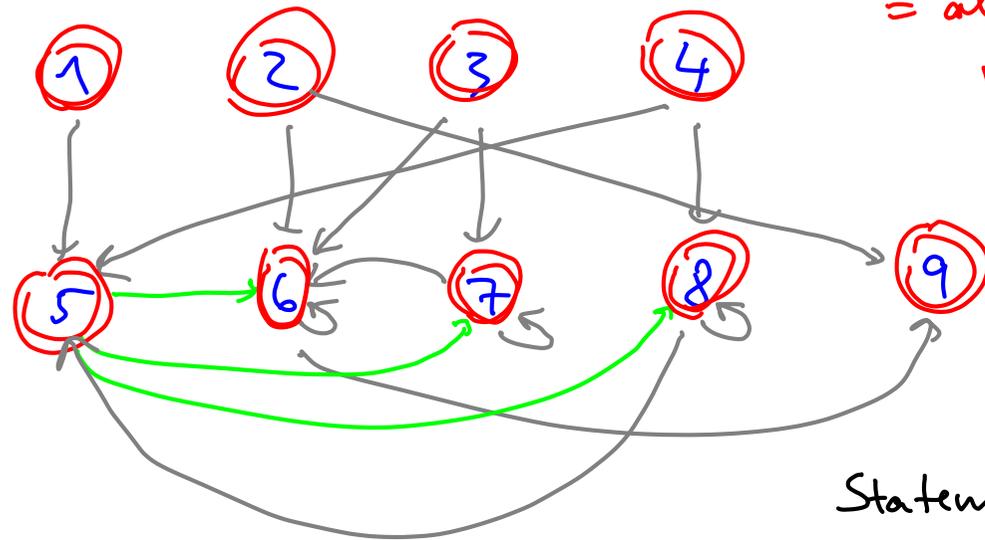
Input:  $n = 1$

History: 1, 2, 3, 4, 5, 6, 7, 8, 9

```

1 var n = readInput();
2 var z = 0;
3 var y = 0;
4 var i = 1;
5 while (i <= n) {
6     z = z + y;
7     y = y + 1;
8     i = i + 1;
9 }
console.log(z);

```



○ .. in history  
 ⊙ .. slice (9, {z})  
 = all statements

BUT:

Statement 7 is not relevant!

# Limitations of Simple Approach

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- **Multiple occurrences** of a single statement are represented as a **single PDG node**
- Difference occurrences of a statement may have **different dependences**
  - All occurrences get **conflated**
- **Slices** may be **larger than necessary**

# Dynamic Slice (Revised Approach)

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## Dynamic dependence graph

- Nodes: Occurrences of nodes of static PDG
- Edges: Dynamic data and control flow dependences

**Slice** for statement  $n$  and variables  $V$  that are defined or used at  $n$ :

- Compute nodes  $S_{dyn}$  that can reach any of the nodes that represent occurrences of  $n$
- Slice = statements with at least one node in  $S_{dyn}$

## Example 2 (Revised approach)

```

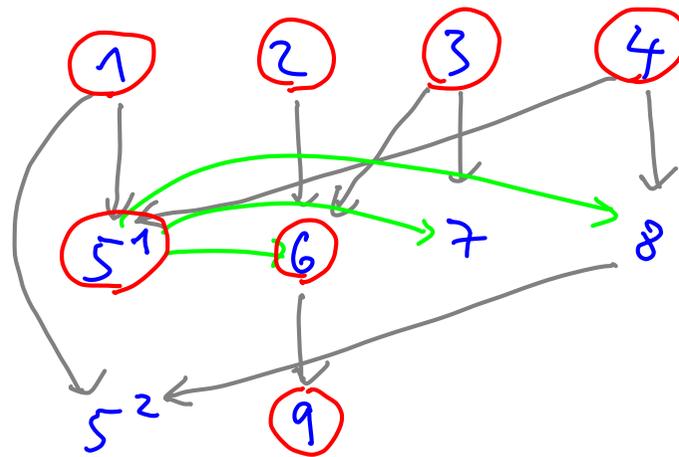
1 var n = readInput();
2 var z = 0;
3 var y = 0;
4 var i = 1;
5 while (i <= n) {
6   z = z + y;
7   y = y + 1;
8   i = i + 1;
9 }
10 console.log(z);

```

Input :  $n = 1$

History : 1, 2, 3, 4, 5, 6, 7, 8, 5, 9

○ .. slice (9, {z})



# Discussion: Dynamic Slicing

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- May yield a program that, if executed, does **not give the same value** for the slicing criterion **than the original program**
- Instead: Focuses on **isolating statements that affect a particular value**
  - Useful, e.g., for debugging and program understanding
- Other approaches exist, see F. Tip's survey for an overview

# Slicing: Summary

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- **Program slicing**: Extract **subset of statements** for a particular **purpose**
  - Debugging, program understanding, change impact analysis, parallelization
- Various techniques
  - **Traditional static slicing**: Executable but potentially very large slice
  - **Thin slicing**: Focus on producer statements, reveal explainer statements on demand
  - **Dynamic slicing**: Useful for understanding behavior of particular execution

# **Program Testing and Analysis: Information Flow Analysis**

**Dr. Michael Pradel**

**Software Lab, TU Darmstadt**

# Outline

---

## 1. Introduction

## 2. Information Flow Policy

## 3. Analyzing Information Flows

## 4. Implementation

Mostly based on these papers:

- *A Lattice Model of Secure Information Flow*, Denning, Comm ACM, 1976
- *Dytan: A Generic Dynamic Taint Analysis Framework*, Clause et al., ISSTA 2007

# Secure Computing Systems

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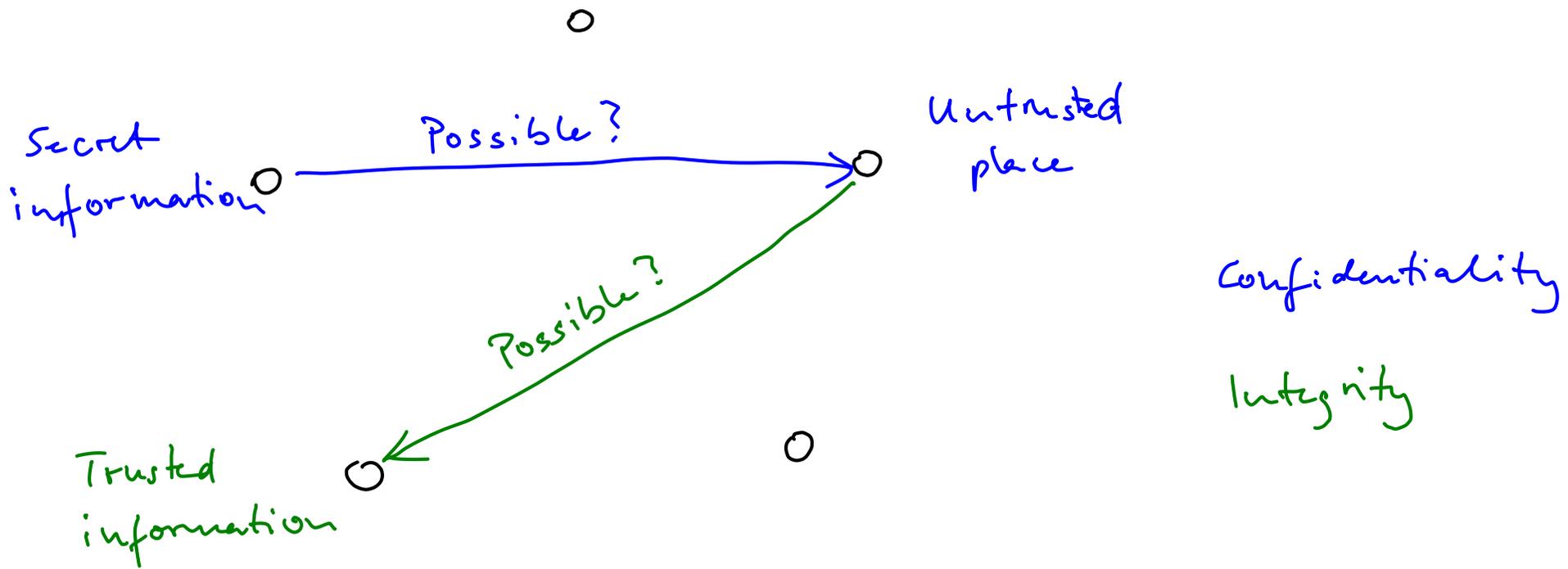
- **Overall goal: Secure the data manipulated by a computing system**
- **Enforce a **security policy****
  - **Confidentiality**: Secret data does not leak to non-secret places
  - **Integrity**: High-integrity data is not influenced by low-integrity data

# Information Flow

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- Goal of **information flow analysis**:  
Check whether information from one "place" **propagates** to another "place"
  - For program analysis, "place" means, e.g., **code location** or **variable**
- **Complements techniques that impose limits on releasing information**
  - Access control lists
  - Cryptography

○ ... "Places" in program that hold data



# Example: Confidentiality

---

**Credit card number should not leak to visible**

```
var creditCardNb = 1234;  
var x = creditCardNb;  
var visible = false;  
if (x > 1000) {  
    visible = true;  
}
```

# Example: Confidentiality

---

Credit card number should not leak to visible

```
var creditCardNb = 1234;  
var x = creditCardNb;  
var visible = false;  
if (x > 1000) {  
    visible = true;  
}
```

Secret information propagates to `x`



Secret information (partly) propagates to `visible`



# Example: Integrity

---

**userInput should not influence who becomes president**

```
var designatedPresident = "Michael";  
var x = userInput();  
var designatedPresident = x;
```

# Example: Integrity

---

**userInput should not influence who becomes president**

```
var designatedPresident = "Michael";  
var x = userInput();  
var designatedPresident = x;
```



Low-integrity information  
propagates to high-integrity  
variable

# Example: Integrity

---

**userInput should not influence who becomes president**

```
var designatedPresident = "Michael";  
var x = userInput();  
if (x.length === 5) {  
    var designatedPresident = "Paul";  
}
```

# Example: Integrity

---

**userInput should not influence who becomes president**

```
var designatedPresident = "Michael";  
var x = userInput();  
if (x.length === 5) {  
    var designatedPresident = "Paul";  
}
```

Low-integrity information propagates to high-integrity variable

# Confidentiality vs. Integrity

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**Confidentiality and integrity are dual problems for information flow analysis**

**(Focus of this lecture: Confidentiality)**

# Tracking Security Labels

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**How to analyze the flow of information?**

- **Assign to each value some meta information that tracks the secrecy of the value**
- **Propagate meta information on program operations**

## Example

```
var creditCardNb = 1234;
var x = creditCardNb;
var visible = false;
if (x > 1000) {
  visible = true;
}
```

secret value

..... = contains secret value

# Non-Interference

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**Property that information flow analysis aims to ensure:**

**Confidential data does not interfere with public data**

- Variation of confidential input **does not cause** a variation of public output
- Attacker **cannot observe any difference** between two executions that differ only in their confidential input

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# Lattice of Security Labels

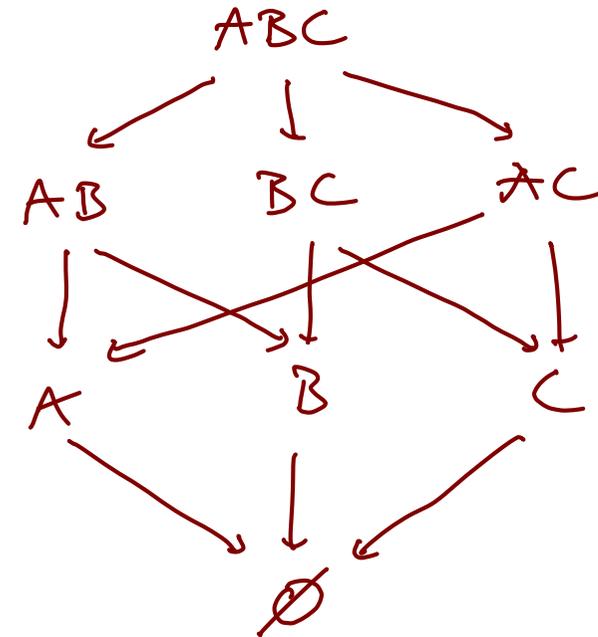
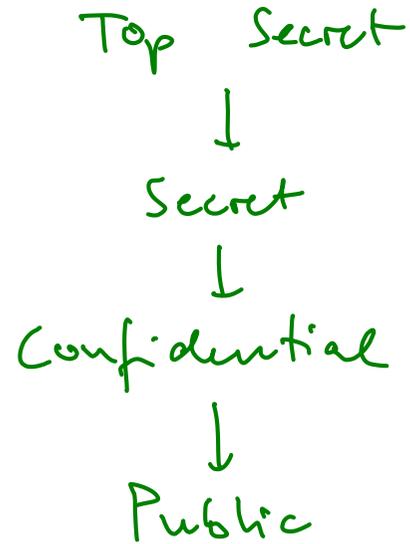
---

How to represent different **levels of secrecy**?

- Set of security labels
- Form a **universally bounded lattice**

## Lattice: Examples

High  
↓  
Low



(Arrows connect more secret class with less secret class.)

## Universally Bounded Lattice

Tuple  $(S, \rightarrow, \perp, \top, \oplus, \otimes)$

where:  $S$  .. set of security classes

$\{ABC, AB, AC, BC, A, B, C, \emptyset\}$

$\rightarrow$  .. partial order  $S$  (see figure)

$\perp$  .. lower bound :  $\emptyset$

$\top$  .. upper bound :  $ABC$

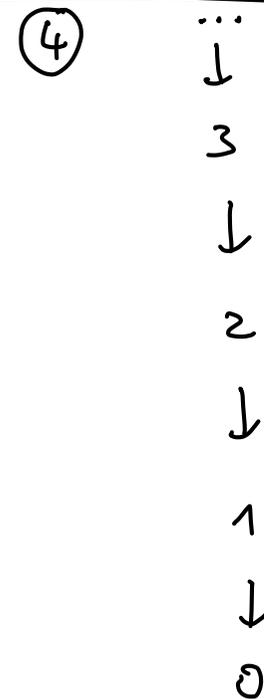
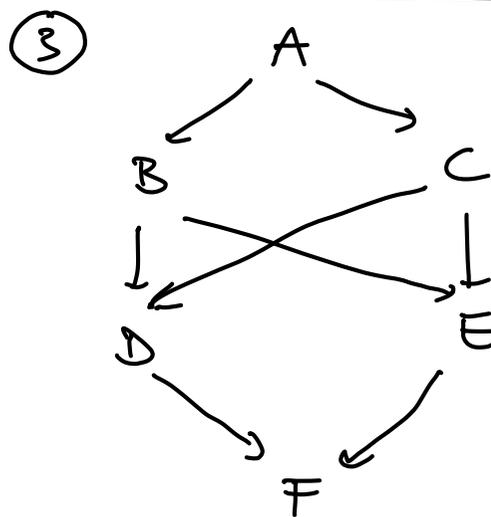
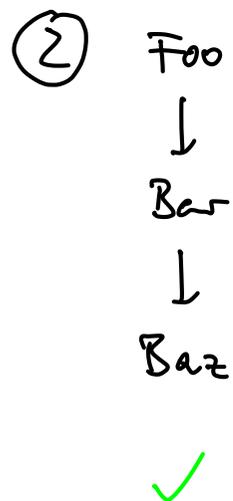
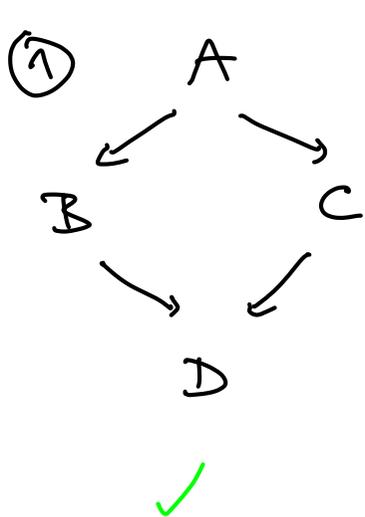
$\oplus$  .. least upper bound operator,  $S \times S \rightarrow S$   
 ("combine two pieces of information")

union, e.g.  $AB \oplus A = AB$ ,  $\emptyset \oplus AC = AC$

$\otimes$  .. greatest lower bound operator,  $S \times S \rightarrow S$

intersection, e.g.  $ABC \otimes C = C$

Quiz: Which of the following is a univ. bounded lattice?



$$D \oplus E = ?$$

three common upper bounds  
(B, C, A), but none  
is the least upper bound

no upper bound  
(infinite)

# Flow Relation

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- Partial order on security classes defines a **flow relation**
- Program is **secure** if and only if **all information flows** are described by the **flow relation**
- Intuition: **No flow from higher to lower security class**

# Information Flow Policy

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Policy specifies **secrecy of values** and which **flows** are allowed:

- Lattice of security classes
- **Sources** of secret information
- Untrusted **sinks**

**Goal:**

**No flow from  
source to sink**

# Information Flow Policy

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Policy specifies **secrecy of values** and which **flows** are allowed:

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**Goal:**

**No flow from source to sink**

```
var creditCardNb = 1234;  
var x = creditCardNb;  
var visible = false;  
if (x > 1000) {  
    visible = true;  
}
```

# Information Flow Policy

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Policy specifies **secrecy of values** and which **flows** are allowed:

- Lattice of security classes
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**No flow from**  
**source to sink**

```
var creditCardNb = 1234;  
var x = creditCardNb;  
var visible = false;  
if (x > 1000) {  
    visible = true;  
}
```

# Declassification

---

- "No flow from high to low" is **impractical**
- E.g., code that checks password against a hash value propagates information to subsequence statements

But: This is intended

```
var password = .. // secret
if (hash(password) === 23) {
    // continue normal program execution
} else {
    // display message: incorrect password
}
```

# Declassification

---

- "No flow from high to low" is **impractical**
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But: This is intended

```
var password = .. // secret
if (hash(password) === 23) {
  // continue normal program execution
} else {
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```

**Declassification: Mechanism to remove or lower security class of a value**

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# Analyzing Information Flows

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Given an information flow policy,  
analysis **checks for policy violations**

## Applications:

- Detect **vulnerable code** (e.g., potential SQL injections)
- Detect **malicious code** (e.g., privacy violations)
- Check if program **behaves as expected** (e.g., secret data should never be written to console)

# Explicit vs. Implicit Flows

---

- **Explicit flows:** Caused by data flow dependence
- **Implicit flows:** Caused by control flow dependence

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# Explicit vs. Implicit Flows

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- **Explicit flows:** Caused by data flow dependence
- **Implicit flows:** Caused by control flow dependence

```
var creditCardNb = 1234;  
var x = creditCardNb;  
var visible = false;  
if (x > 1000) {  
    visible = true;  
}
```

Explicit flow from  
creditCardNb to x

Implicit flow from  
x > 1000 to visible

# Explicit vs. Implicit Flows

---

- **Explicit flows:** Caused by data flow dependence  
Some analyses consider only these
- **Implicit flows:** Caused by control flow dependence

```
var creditCardNb = 1234;
var x = creditCardNb;
var visible = false;
if (x > 1000) {
    visible = true;
}
```

Explicit flow from creditCardNb to x

Implicit flow from x > 1000 to visible

# Static and Dynamic Analysis

---

## ■ **Static information flow analysis**

- **Overapproximate** all possible data and control flow dependences
- Result: Whether information "**may flow**" from secret source to untrusted sink

## ■ **Dynamic information flow analysis**

- Associate security labels ("**taint markings**") with **memory locations**
- **Propagate** labels at **runtime**

# Static and Dynamic Analysis

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- **Static information flow analysis**

- **Overapproximate** all possible data and control flow dependences
- Result: Whether information "**may flow**" from secret source to untrusted sink

- **Dynamic information flow analysis**

- Associate security labels ("**taint markings**") with **memory locations**
- **Propagate** labels at **runtime**

**Focus of rest of this lecture**

# Taint Sources and Sinks

---

## ■ Possible sources:

- Variables
- Return values of a particular function
- Data from a type of I/O stream
- Data from a particular I/O stream

# Taint Sources and Sinks

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## ■ Possible sources:

- Variables
- Return values of a particular function
- Data from a type of I/O stream
- Data from a particular I/O stream

## ■ Possible sinks:

- Variables
- Parameters given to a particular function
- Instructions of a particular type (e.g., jump instructions)

# Taint Sources and Sinks

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## ■ Possible sources:

- Variables
- Return values of a particular function
- Data from a type of I/O stream
- Data from a particular I/O stream

## ■ Possible sinks:

- Variables
- Parameters given to a particular function
- Instructions of a particular type (e.g., jump instructions)

**Report illegal flow if taint marking flows to a sink where it should not flow**

# Taint Propagation

---

## 1) **Explicit flows**

**For every operation that produces a new value, propagate labels of inputs to label of output:**

$$label(result) \leftarrow label(inp_1) \oplus \dots \oplus label(inp_2)$$

# Taint Propagation (2)

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## 2) Implicit flows

- Maintain **security stack  $S$** : Labels of all values that influence the current flow of control
- When  $x$  influences a **branch decision** at location  $loc$ , **push**  $label(x)$  on  $S$
- When control flow reaches **immediate post-dominator** of  $loc$ , **pop**  $label(x)$  from  $S$
- When an operation is executed while the  $S$  is non-empty, consider all **labels on  $S$  as input** to the operation

## Example 1

Policy:

- security classes: public, secret
- source: variable "creditCardNb"
- sink: variable "visible"

```

var creditCardNb = 1234;
var x = creditCardNb;
var visible = false;
if (x > 1000) {
  visible = true;
}

```

$Label(\text{creditCardNb}) = \text{secret}$   
 explicit flow:  $Label(x) = \text{secret}$   
 $Label(\text{visible}) = \text{public}$   
 produce intermediate value  $b$ ,  
 $Label(b) = Label(x) \oplus Label(1000)$   
 $= \text{secret} \oplus \text{public} = \text{secret}$   
 push secret on  $S$   
 labels on  $S$  are part of input  
 $Label(\text{visible}) = \text{secret} \oplus Label(\text{true})$   
 $= \text{secret}$   
 $\rightarrow$  violation of policy

# Example 2: Quiz

---

```
var x = getX();  
var y = x + 5;  
var z = true;  
if (y === 10)  
    z = false;  
foo(z);
```

## Policy:

- Security classes: public, secret
- Source: `getX`
- Sink: `foo()`

**Suppose that `getX` returns 5. Write down the labels after each operation.**

**Is there a policy violation?**